

# Math 103 Day 22: Exponential Functions and their Derivatives

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# Outline

## 1 Exponential Functions and their Derivatives

# Properties of Exponential Functions

- 1 If  $a > 0$ , then  $a^{x+y} = a^x a^y$ .
- 2 If  $a > 0$ , then  $a^{x-y} = \frac{a^x}{a^y}$ .
- 3 If  $a > 0$ , then  $(a^x)^y = a^{xy}$ .
- 4 If  $a > 0$  and  $b > 0$ , then  $(ab)^x = a^x b^x$ .
- 5 If  $a > 1$ , then  $\lim_{x \rightarrow \infty} a^x = \infty$  and  $\lim_{x \rightarrow -\infty} a^x = 0$ .
- 6 If  $0 < a < 1$ , then  $\lim_{x \rightarrow \infty} a^x = 0$  and  $\lim_{x \rightarrow -\infty} a^x = \infty$ .